## Chronotaxic systems

## Systems far from thermodynamic equilibrium that adjust their clocks

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Herman Haken's Symposium
HWK, 13-16 Novmber, 2012

## Outline

(1) Collaborators
(2) The approach

- Analyses
- The cardiovascular system brings fuel to each cell
- Origin of biological oscillations?
- The brain controls/supervises each cell
(3) Characterising the dynamics
- Systems with time-varying parameters

4. Novel methods are needed

- Additional motivation
- Dynamical inference
(5) Chronotaxic systems


## People in Nonlinear and Biomedical Physics

- Academic staff
- Prof Aneta Stefanovska
- Prof Peter McClintock
- Dr Dmitry Luchinsky
- Research Associates
- Dr Tomislav Stankovski
- Dr Yevhen Suprunenko
- Dr Rodrigue Tindjong
- PhD students
- Ms Suhir Abuhajar
- Mr Phil Clemson
- Mr Tom Hansard
- Mr Dima latsenko
- Ms Gemma Lancaster
- Mr Shakil Patel
- Mr Spase Petkoski
- Mr Norman Turner



## A longstanding and ambitious goal

- More than 20 years of work on the question What are physical principles of living systems?
- The work involves
- theory of coupled oscillators
- development of novel numerical methods to analyse dynamics from recorded data
- development and applications of novel recording/imaging methods
- applications
- Many collaborators in almost all continents.
- With greatest thanks to Professor Hermann Haken


## Insight from measured signals



The approach: combining theory, measurements and a priori knowledge to extract the basic dynamical principles of life.

## Analysis

- Time domain; methods for decomposition, like independent component analysis, principal component analysis, non-linear mode decomposition...
- Frequency domain, i.e. Fourier transform, bispectral analysis
- Time-frequency domain, i.e. wavelet transform, wavelet-based bispectral analysis, ...
- Phase space, i.e. Lyapunov exponents, correlation dimension
- Complexity analysis, i.e. Fractal and multifractal analysis, Horst exponent, entropy-based measures, Fokker-Planck analysis ${ }^{1}$
- Methods for analysis of interactions, i.e. synchronization, coherence, direction of coupling.

[^0]
## Time series analysis

- Wavelet transform - transformation from time to the time-frequency domain

- Morlet mother wavelet $\Rightarrow$ family of wavelets
- Time resolution: shifting the wavelet along the signal
- Frequency resolution: stretching/shortening of the wavelet
- Continuous WT - tracing the oscillations in time


## Wavelet transform



- WT coefficients in the time-frequency plane
- Six peaks in the interval from 0.005 Hz to 2 Hz
- Average wavelet transform with interval boundaries
- Logarithmic frequency resolution



## Time scales in humans

Cardiovascular oscillations


Stefanovska, Coupled oscillators - Complex but not complicated cardiovascular and brain interactions, IEEE Eng Med Biol Mag 26: 25-29, 2007.

## Non-excitable cells

- Non-excitable cells have time-dependent properties and functions, e.g. vascular endothelial cells.
- The action potential is a special case of membrane dynamics only observed in nerve and muscle cells.
- The vast amount of information in the subtle fluctuations of the membrane potential has been left unexplored.



## Mitochondrial oscillations

Experiments have found that the membrane potentials of mitochondria oscillate at a frequency $\sim 10 \mathrm{mHz}$.


Ref: FT Kurz, MA Aon, B O'Rourke and

## Whole Cell

(patch clamp)



Ref: PT Clemson et al, Proc ESGCO 2010, (2010)

## Astrocytes - linking the CVS with brain dynamics




- Glial cells provide nutrition for the neurons.
- They couple the cardiovascular oscillations to brain waves.


## Impact

## Clinical studies

- Hypertension (RLI, Pisa)
- Post myocardial infarction (Ljubljana)
- Heart failure (RLI)
- Diabetes mellitus (Ljubljana)
- Brain injury critical care (Oslo)
- Tetraplegia (Mt Sinai Hospital, NY)
- Cancer (Pisa, RLI)


## States

- Anæsthesia (RLI, Ljubljana, Olso)
- Ageing (Ljubljana, RLI)
- Exercise (Oslo, Physics Department)
- Breath-hold (Physics Department)
- Part or whole body heating (Physics Department, Nagoya, Virginia)


## Ways to treat living systems

Various approaches to living systems, in particular to treat them as -

- Stochastic? No. Although random fluctuations can be important, the underlying dynamics is not stochastic
- Chaotic? No. Again, the ideas of chaos theory do not describe well a dynamics that exhibits a lot of determinism
But their parameters vary in time... If the variations are caused by external influences, can treat them as -
- Non-autonomous? Yes...

The mathematical theory of non-autonomous systems is potentially able to provide an excellent description of the parameter variations observed in living systems.

## Complex oscillations in the cardiovascular system



Bračič Lotrič, Stefanovska, Physica A 283: 451-461, 2000
Stefanovska, Haken, McClintock, et al, Phys Rev Lett 85: 4831-4834, 2000 Jamšek, Stefanovska, McClintock, Phys Med Biol 49: 4407-4425, 2004 Bahraminasab, Kenwright, Stefanovska, et al, IET Syst Biol 2: 48-54, 2008
Kenwright, Bahraminasab, Stefanovska, McClintock, Eur Phys J B 65: 425-433, 2008
Shiogai, Stefanovska, McClintock, Phys Rep 488: 51-110, 2010

## Dynamical inference

- Inverse problem - starting from time series, one tries to understand the dynamics of interacting oscillators in nature
- Time-variability of parameters presents an almost inevitable challenge

Cardio-respiratory interactions


- Questions raised
- Why qualitative transitions exist (from 1:4 to 1:5 to 1:6 ratio, sync to no-sync)?
- Is it because the frequency or the coupling parameter is time-varying?
- Are the parametric and/or functional relationships influenced?


## Main Concept

Phase time-series from noisy interacting oscillators


## Phase dynamics and base functions

- When $N$-dimensional limit cycle oscillators $d \mathbf{x}_{i} / d t=\mathbf{f}_{i}\left(\mathbf{x}_{i}(t)\right)$ interact weakly, it is common to describe their motion by their respective phase dynamics:

$$
\dot{\phi}_{i}=\omega_{i}+f_{i}\left(\phi_{i}\right)+q_{i}\left(\phi_{i}, \phi_{j}\right)+\xi_{i}
$$

- Periodic solution $\rightarrow$ periodic base functions
- Fourier series to decompose both $f_{i}$ and $q_{i}$ :

$$
\begin{aligned}
f_{i}\left(\phi_{i}\right) & =\sum_{k=-\infty}^{\infty} \tilde{c}_{i, 2 k} \sin \left(k \phi_{i}\right)+\tilde{c}_{i, 2 k+1} \cos \left(k \phi_{i}\right) \\
q_{i}\left(\phi_{i}, \phi_{j}\right) & =\sum_{s=-\infty}^{\infty} \sum_{r=-\infty}^{\infty} \tilde{c}_{i ; r, s} e^{i 2 \pi r \phi_{i}} e^{i 2 \pi s \phi_{j}}
\end{aligned}
$$

- Approximation to finite number $K$ of selected Fourier terms:

$$
\dot{\phi}_{l}=\sum_{k_{i}=-K}^{K} c_{k_{i}}^{(I)} \Phi_{l, k_{i}}\left(\phi_{1}, \phi_{2}\right)+\xi_{l}(t)
$$



Stankovski, Duggento, McClintock, Stefanovska, Inference of time-evolving coupled dynamical systems in the presence of noise, Phys Rev Lett 109: 024101, 2012.

Time-evolution of coupling functions from cardio-respiratory interactions


## Coupling function

$$
\begin{aligned}
& \dot{\phi}_{h}=\omega_{h}+q_{h}\left(\phi_{h}, \phi_{r}\right)+\xi_{h} \\
& \dot{\phi}_{r}=\omega_{r}+q_{r}\left(\phi_{h}, \phi_{r}\right)+\xi_{r}
\end{aligned}
$$

Time-averaged coupling function of heart $\left(q_{h}\right)$ and respiration $\left(q_{r}\right)$


The heart coupling function is dominated by RSA, which decreases with age, whereas the respiratory coupling function seems to be irregular and unaffected by age.
latsenko et al, Evolution of cardio-respiratory interactions with age, Phil Trans A, accepted.

## Chronotaxic systems

We have identified a new family of dynamical systems: self-sustained oscillators subject to deterministic (periodic) parametric modulation -

- Chronotaxic systems:
- From chronos (time) + taksi (order, class)
- Deterministic
- Explicitly time-dependent
- Non-chaotic
- Mathematically:

$$
\frac{d \mathbf{x}}{d t}=f\left(\mathbf{x}\left(\mathbf{t}_{0}\right), t_{0}, t\right)
$$

The additional dependence on $t_{0}$ is the defining characteristic.

- Nature abounds with chronotaxic systems
- Observed also in physical systems: similar, reproducible dynamics have been measured in the currents of surface state electrons on liquid helium.


## Physical context of chronotaxic systems



## Stochastic versus chronotaxic

Stochastic forcing


Quasi-periodic forcing




## Inverse problems

When given only a single time series from a chronotaxic system, a time-dependent representation can reveal the hidden limit cycle behaviour and stability of the system parameters.


## Chronotaxic systems

- The time-dependent perturbations of a self-sustained oscillatory system can result in a complex dynamics.
- Under such perturbations the stability evident in the unperturbed limit cycle may be lost.
- However the chronotaxic systems are able to retain their stability through the time dependent adjustments of the initial limit cycle.


## Limit cycle

- Limit cycle in autonomous systems. Example 1:

$$
\left\{\begin{array}{l}
\dot{r}=2-r \\
\dot{\varphi}=\omega_{0}
\end{array}\right.
$$

Limit cycle $r^{*}=2$.

- Under the time-dependent perturbation
 limit cycle becomes time-dependent, if limit cycle still exists.



## The time-dependent adjustments of the limit cycle

- Example 2:

$$
\left\{\begin{array}{l}
\dot{r}=2-r+F(t) \\
\dot{\varphi}=\omega_{0}
\end{array}\right.
$$

Typical trajectory:


Time-dependent perturbation:

$$
F(t)=\sin (\sqrt{2} t)+\sqrt{2} \cos (\sqrt{2} t)
$$

Time-dependent limit cycle:

$$
r^{*}(t)=2+\sin (\sqrt{2} t)
$$

If using $r^{*}(t)$ :


## Summary

- Chronotaxic systems are not new (they also fall under old categories, e.g. non-autonomous).
- But they have certain features which allow us to put them in a separate class that we now define.
- Chronotaxic systems retain their stability. When perturbed, their limit cycles are not destroyed but can instead become time-dependent.
- Instead of the traditional view of this type of dynamics as stochastic, we now propose a new class of systems that categorizes them as deterministic.


## Summary continued

- Benefits for theory: once we are aware that chronotaxic systems may exist, it is reasonable to improve the existing descriptions of systems with time-dependent limit cycles, e.g.
- the identification of time-dependent limit cycles and corresponding parameters,
- amplitude and phase separation.
- Benefits for inverse problem approach: avoid misinterpreting these systems as stochastic; further develop appropriate methods to capture their time variability.


[^0]:    ${ }^{1}$ A. Bahraminasab, F. Ghasemi, A. Stefanovska, P.V.E. McClintock, R. Friedrich. Physics of brain dynamics: Fokker-Planck analysis reveals changes in EEG $\delta-\theta$ interactions in anæsthesia. NJP 11: 103051, 2009.

