

# Phase transitions in ferromagnetic monolayers: A playground to study fundamentals

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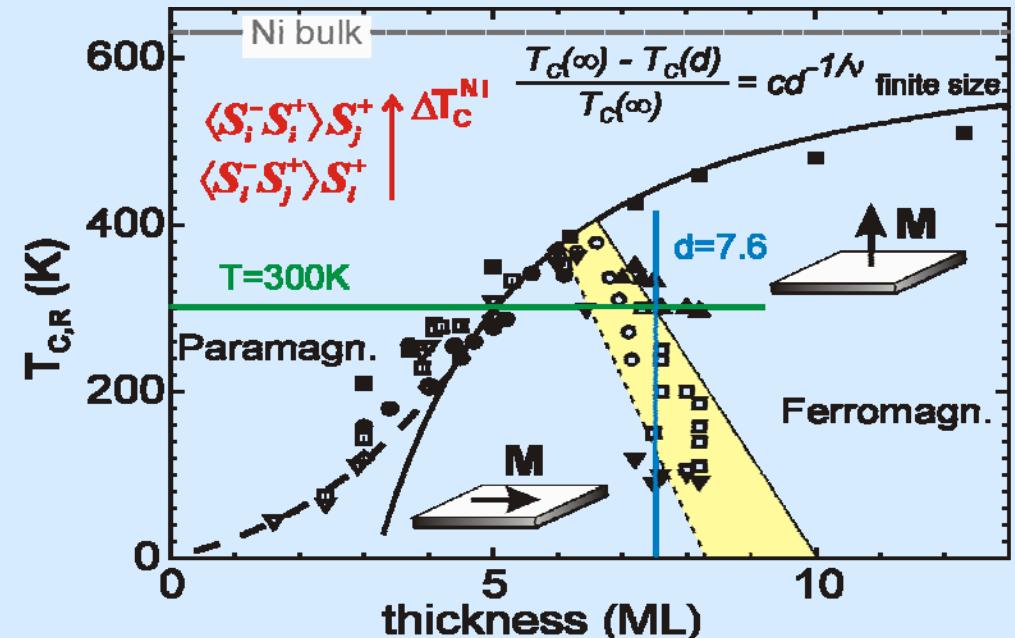
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<http://www.physik.fu-berlin.de/~bab>

- $T_{\text{crit}}$ , Phase Transitions
- Spin Reorientation Transition Magnetic Anisotropy Energy
- Manipulation of the SRT
- Summary, Take Home



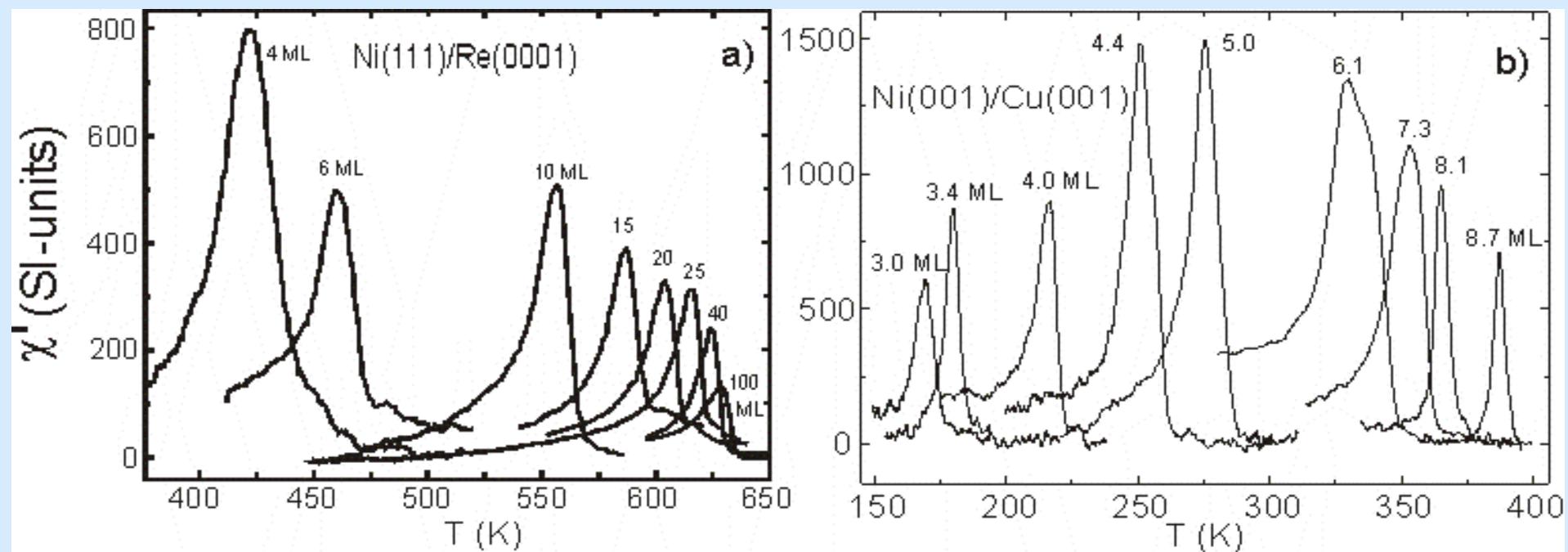
## Para- to ferromagnetic phase transition, Curie temperature,

Bulk Fe, Co, Ni have only one  $T_C$ , each (few % changes are possible).

For ultrathin films  $T_C$  can be manipulated from zero to  $T_C^{\text{bulk}}$ .

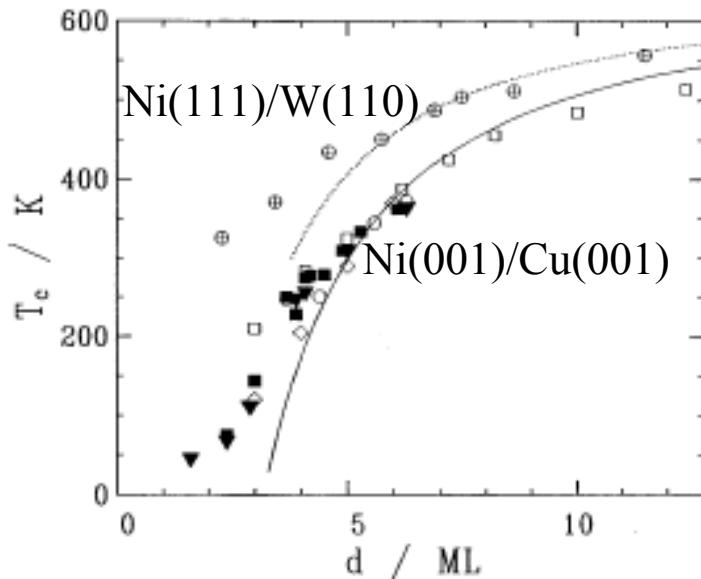
**New and Great !**

How do we measure  $T_C$ ?  $\chi_{\text{ac}}$  increases at  $T_C$ ; dc-MOKE vanishes!



**“Magnetism in thin films”**

P. Poulopoulos, K. B., J. Phys. Condens. Matter. **11**, 9495 (1999)



**Fig. 7.** Critical temperature  $T_c$  for: Ni (111)/W (110)  $\oplus$  [6], and Ni (001)/Cu (001) dc-MCXD ( $\blacktriangledown$ ), ac-MCXD  $\blacksquare$  [15], and  $\square$  [14],  $\circ$  [26],  $\diamond$  [25]. The solid and dotted lines are fits to (8) with values for  $c$  given in the text

$$\frac{T_c(\infty) - T_c(d)}{T_c(\infty)} = cd^{-1/\nu}$$

finite size scaling,

If  $T_c$  changes the reduced temperature  $T/T_c = t$  is important.

Different  $T_c$  for Ni(111) and Ni(001). How can this be explained ?

For the same ferromagnet but different surface orientation, we keep the critical exponent  $\nu$  fixed to be  $\nu = 0.705$  (Heisenberg). A 15% rescaling for the different layer spacing for the (111) film ( $\oplus$ ) was used. The only parameter left to be adjusted for the 2 films [(111) dotted line, (001) full line] is the coefficient  $c$ . The ratio of

$$\frac{c^{(111)}}{c^{(001)}} = \frac{3.6}{5.2} = \boxed{0.69}$$

agrees perfectly with:

$$\frac{\Delta N^{(111)}}{\Delta N^{(001)}} = \frac{3}{4} = \boxed{0.75}.$$

K. B. Appl. Phys. A **62**, 417 (1996) #171

## Superconductor/ferromagnet proximity effect in Fe/Pb/Fe trilayers

L. Lazar, K. Westerholt, and H. Zabel

*Institut für Experimentalphysik/Festkörperphysik, Ruhr-Universität Bochum, 44780 Bochum, Germany*

L. R. Tagirov

*Kazan State University, 420008 Kazan, Russian Federation*

Yu. V. Goryunov, N. N. Garif'yanov, and I. A. Garifullin

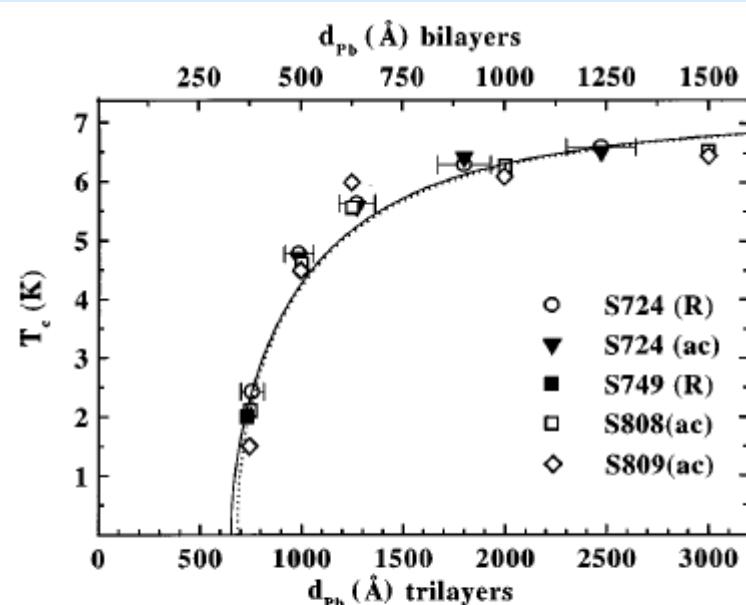
*Kazan Physicotechnical Institute, Russian Academy of Sciences, 420029 Kazan, Russian Federation*

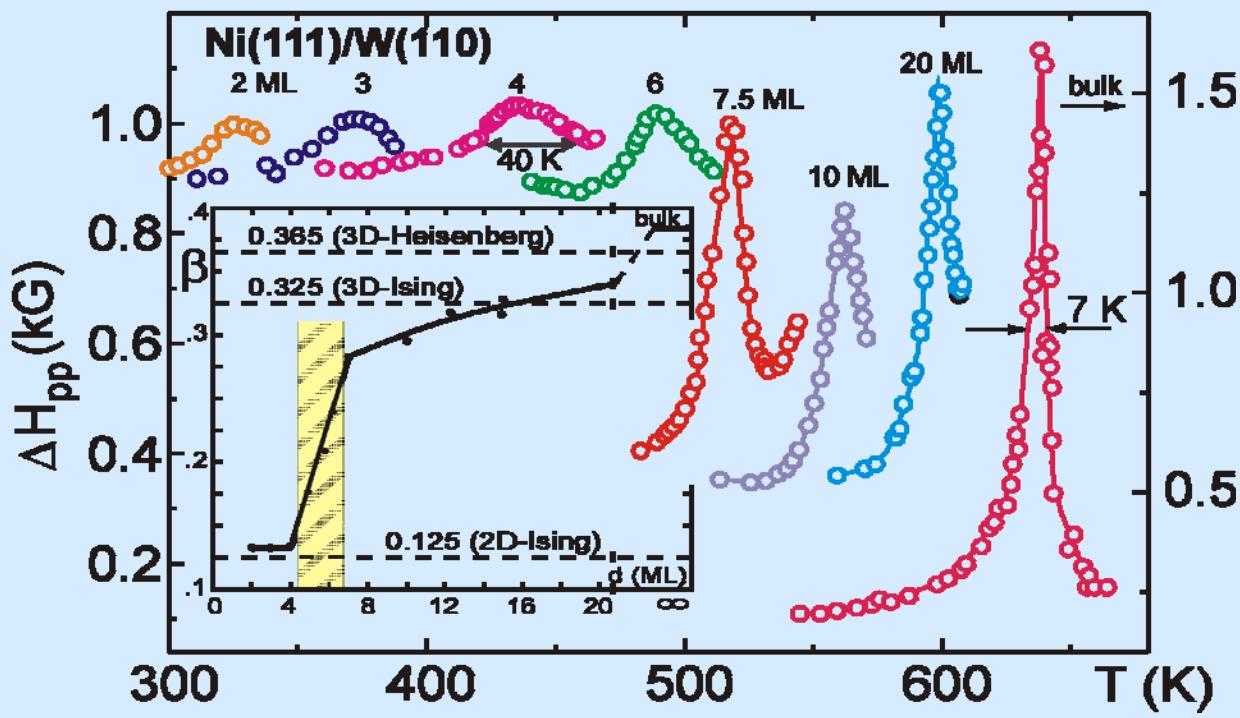
FIG. 7. Dependence of the superconducting transition temperature on the thickness of the Pb-layer for four sample series listed in Table I. The dotted and solid lines are the best fits using the theory by Radović *et al.* and the theory by Tagirov, respectively, with parameters given in the figure subscripts of Figs. 10 and 11.

Finite size scaling is a general phenomenon and not specific for FM.

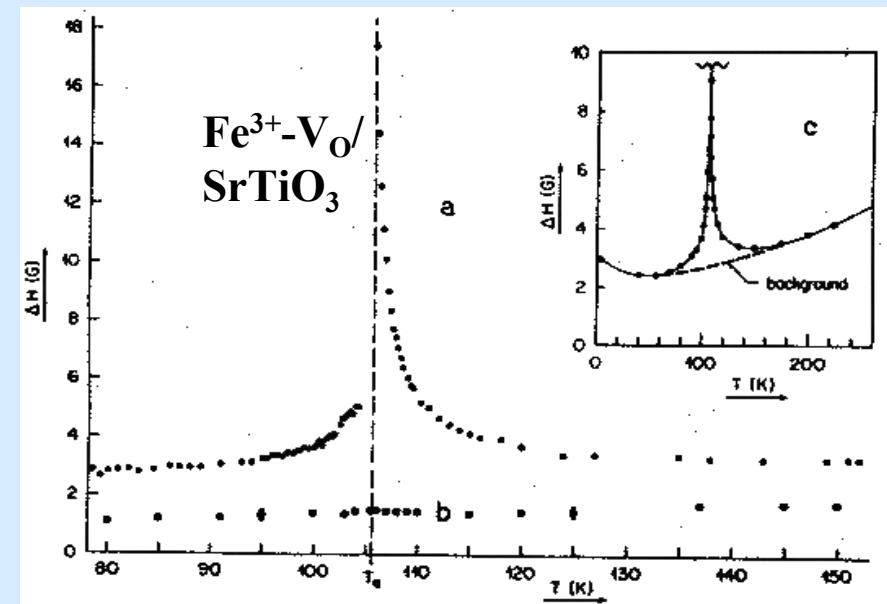
The difference lies in the different correlation lengths  $\xi$ .

$$\xi = \xi_0 (1-t)^{-\nu}$$

Close to  $T_C$  fluctuations (Gaussian or critical) increase.  
 This increases the linewidth in magnetic resonance spectroscopy.

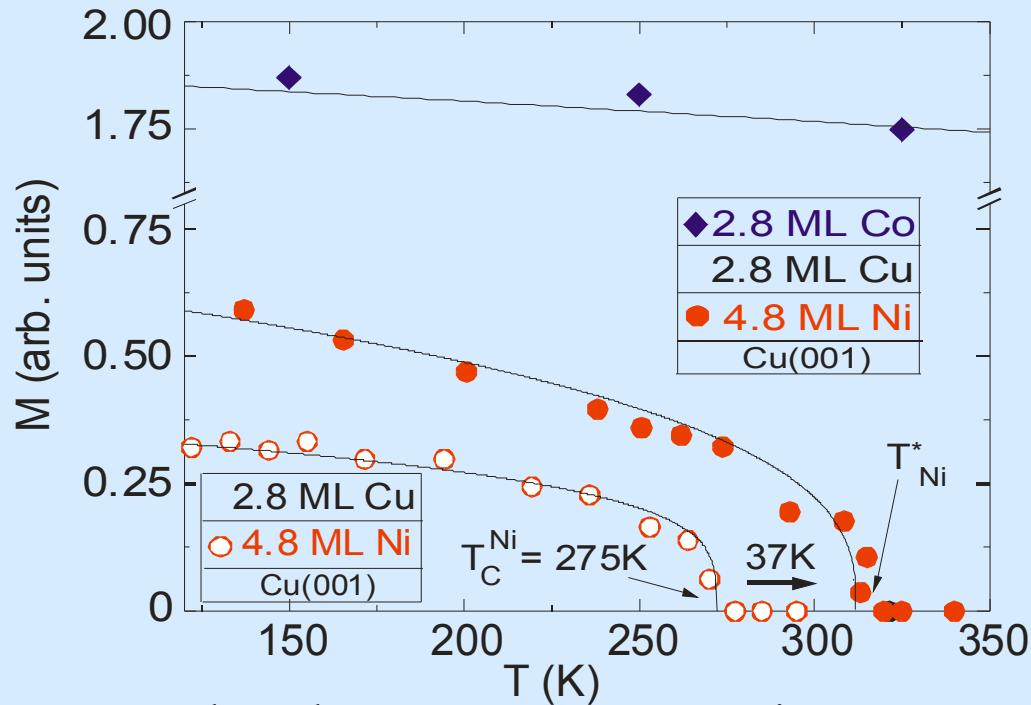


Yi Li, K. B., PRL 68, 1208 (1992) #126

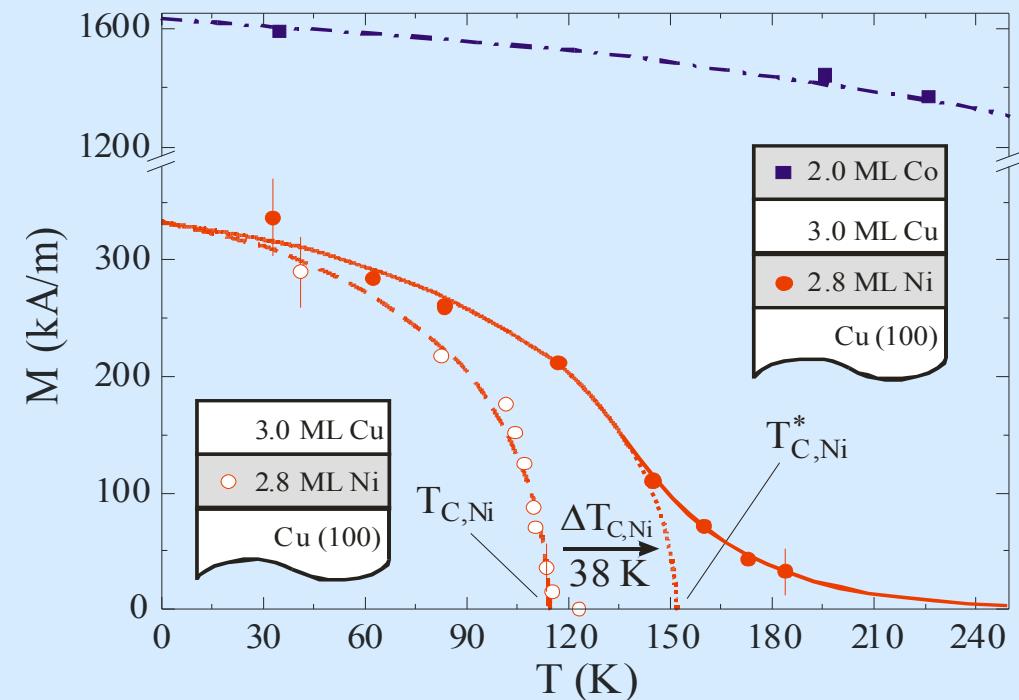


Th.v. Waldkirch, K.A. Müller,  
 W. Berlinger, PRB (1973)

# Element specific UHV-XMCD measurements



P. Poulopoulos, K. B., Lecture Notes in Physics **580**, 283 (2001)

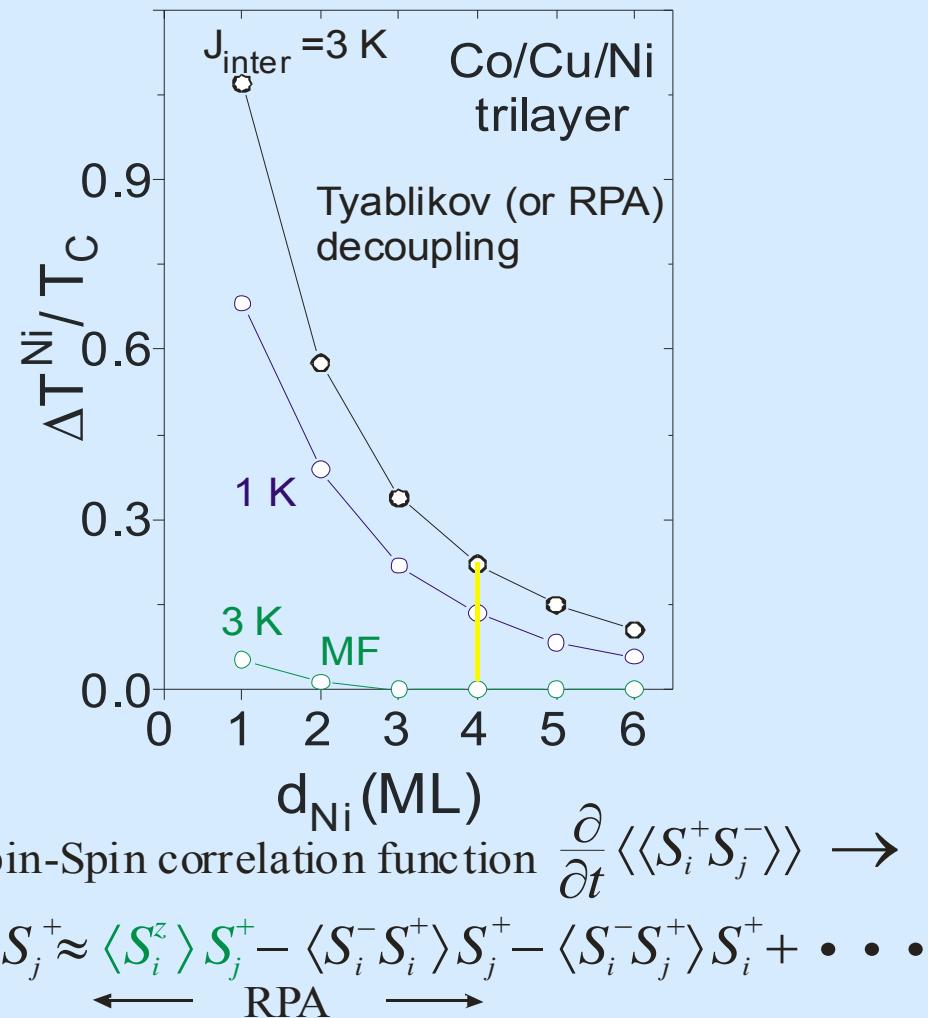


A. Scherz et al. PRB **65**, 24411 (2005)

The large shift of  $T_C^{Ni}$  can **NOT** be explained by the static exchange field of Co.

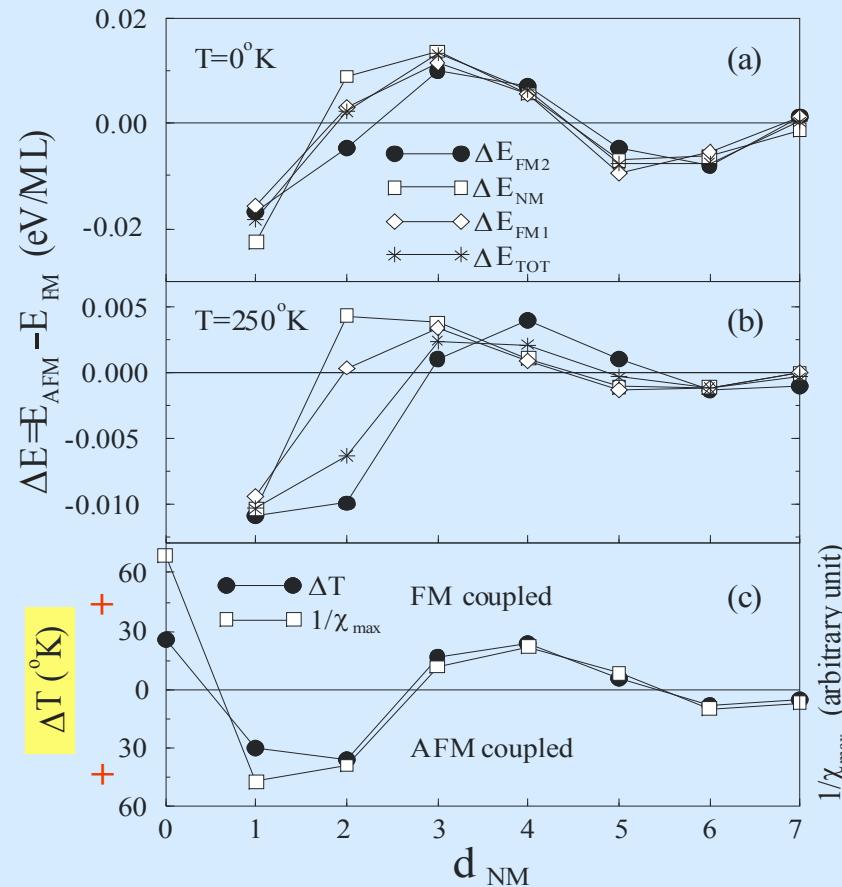
# Enhanced spin fluctuations in 2D (theory)

P. Jensen et al. PRB **60**, R14994 (1999)



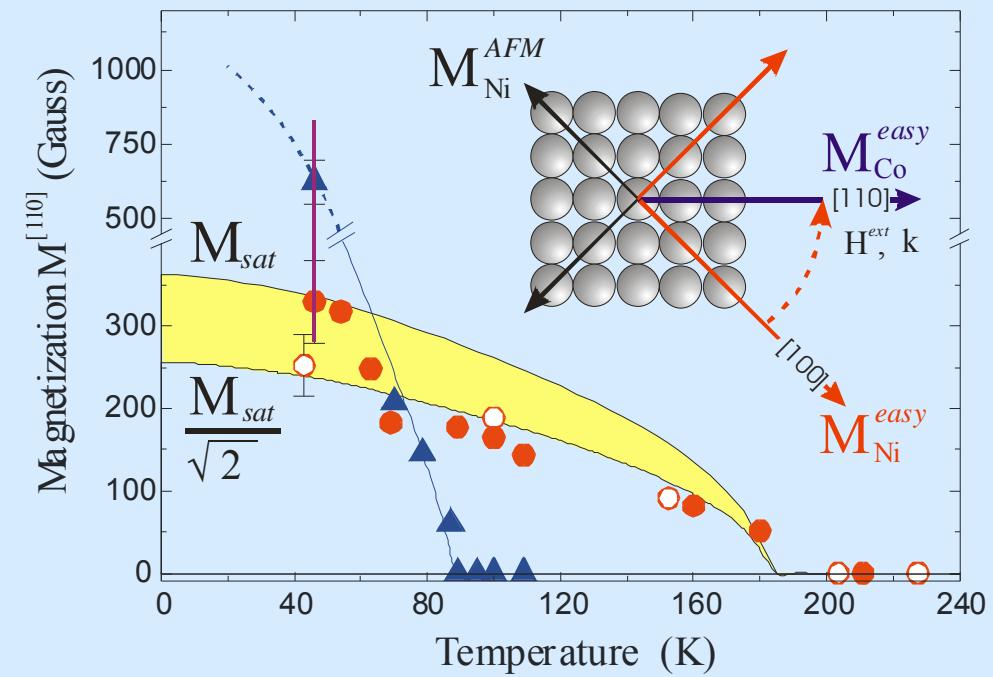
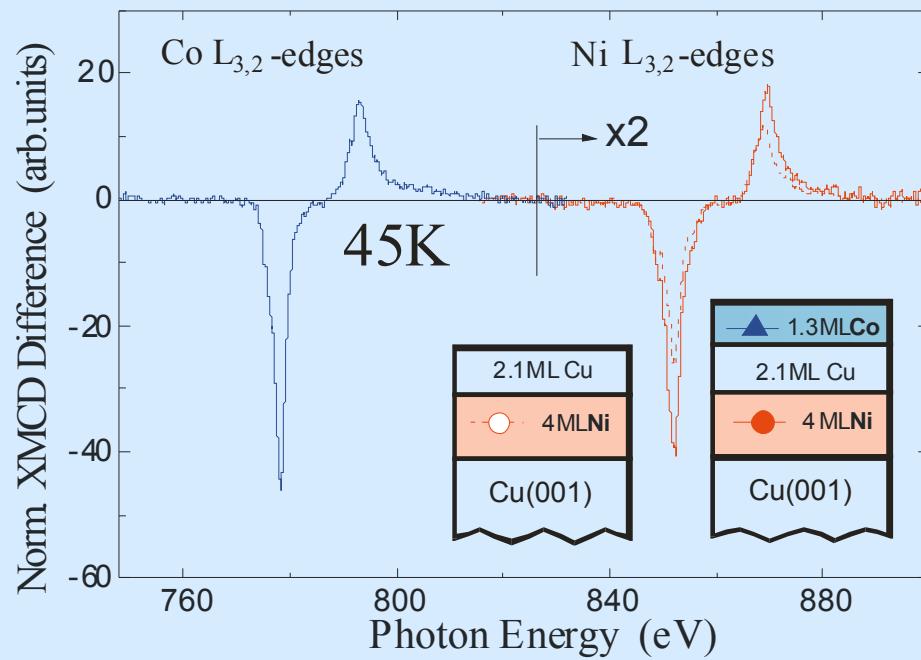
$\langle S_i^z \rangle S_j^+$ , mean field ansatz (Stoner model) is insufficient to describe spin dynamics at interfaces of nanostructures

J.H. Wu et al. J. Phys.: Condens. Matter **12** (2000) 2847



Single band Hubbard model:  
Simple Hartree-Fock ansatz is insufficient  
Higher order correlations are needed to explain  $T_C$ -shift

# Two phase transitions at $T_c^{Ni}$ and $T_c^{Co}$ ?



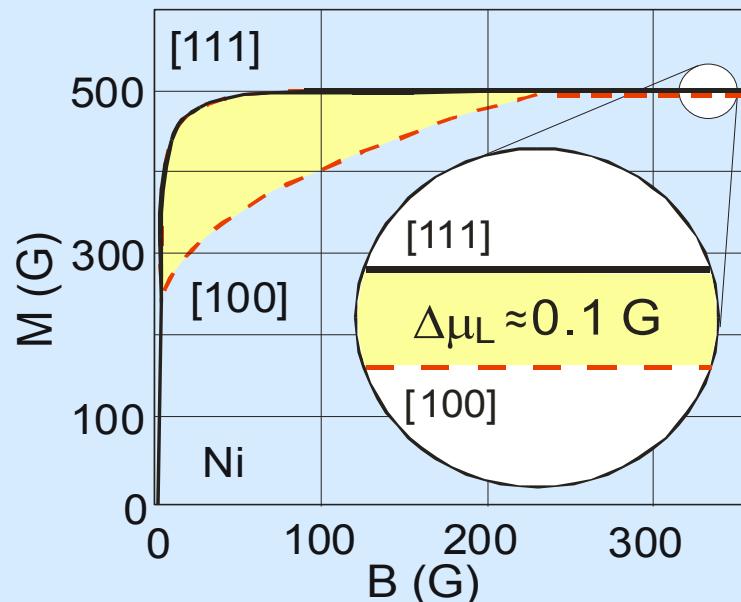
Crossover of  $M_{Co}(T)$  and  $M_{Ni}(T)$

A further reduction in symmetry happens at  $T_c^{\text{low}}$

A. Scherz et al. J. Synchrotron Rad. **8**, 472 (2001) #248, 245

# Magnetic Anisotropy Energy (MAE)

1. Magnetic anisotropy energy =  $f(T)$
2. Anisotropic magnetic moment  $\neq f(T)$



$$\text{MAE} = \int M \cdot dB \approx \frac{1}{2} \Delta M \cdot \Delta B \approx \frac{1}{2} 200 \cdot 200 \text{ G}^2$$

$$\text{MAE} \approx 2 \cdot 10^4 \text{ erg / cm}^3 \approx 0.2 \text{ } \mu\text{eV / atom}$$

*Characteristic energies of metallic ferromagnets*

binding energy	1 - 10 eV/atom
exchange energy	10 - $10^3$ meV/atom
cubic MAE (Ni)	0.2 $\mu\text{eV}/\text{atom}$
uniaxial MAE (Co)	70 $\mu\text{eV}/\text{atom}$

K. B. Lecture Notes in Physics, Springer **580**, 27 (2001)

$\approx 1 \mu\text{eV}/\text{atom}$  is very small compared to  
 $\approx 10 \text{ eV}/\text{atom}$  total energy **but all important**

# The origin of MAE

There are only 2 origins for MAE: 1) dipol-dipol interaction  $\sim (\bar{\mu}_1 \cdot \bar{r})(\bar{\mu}_2 \cdot \bar{r})$  and

2) spin-orbit coupling  $\lambda \bar{L} \bar{S}$  (intrinsic K or  $\Delta E_{\text{band}}$ )

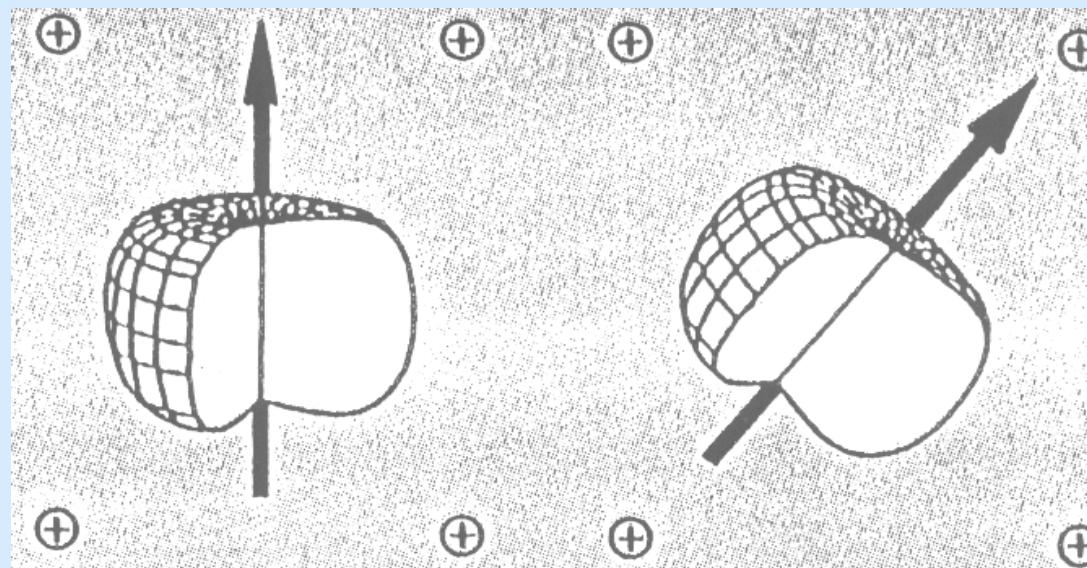


Abb. 3: Die Vorzugsrichtung des magnetischen Moments (leichte Richtung) der intermetallischen Seltenerdverbindungen hat ihre Ursache in der starren Kopplung zwischen magnetischem Moment (Pfeil) und Ladungsverteilung der 4f-Elektronen des Neodym. Bei einer Rotation des magnetischen Moments aus der c-Richtung (senkrecht) heraus dreht sich die anisotrope Ladungswolke mit. Da die Wechselwirkungsenergie zwischen 4f-Ladungswolke und Ladungswolken der benachbarten Ionen ( $\oplus$ ) dabei zunimmt, wird die leichte Richtung favorisiert.

Aus der Wissenschaft

Phys. Bl. 53 (1997)

Superstarke Magnete  
intermetallischer Verbindungen der Seltenerdmetalle  
Leistungssteigerung durch nanokristalline Strukturen

H. Kronmüller

# Free energy density of MAE, K

(intrinsic, after subtraction of the shape anisotropy  $2\pi M^2$ )

**tetragonal [e.g. Ni, Co, Fe (001) / Cu (001) ]:**

$$\begin{aligned} E_{\text{tetr}} &= -K_2 \cos^2\theta & -\frac{1}{2} K_{4\perp} \cos^4\theta - \frac{1}{2} K_{4||} \frac{1}{4} (3 + \cos 4\phi) \sin^4\theta + \dots & (\text{Bab et al.}) \\ &= (K_2 + K_{4\perp}) \sin^2\theta & -\frac{1}{2} (K_{4\perp} + \frac{3}{4} K_{4||}) \sin^4\theta - \frac{1}{8} K_{4||} \cos 4\phi \sin^4\theta + \dots \\ &= K_2' \sin^2\theta & + K_{4\perp} \sin^4\theta + K_{4||} \cos 4\phi \sin^4\theta + \dots & (\text{traditional}) \end{aligned}$$

**hexagonal [e.g. Ni (111), Gd (0001) / W (110) ]:**

$$E_{\text{hex}} = k_2 \sin^2\theta + \frac{1}{2} k_{2||} \cos 2\phi \sin^2\theta + k_4 \sin^4\theta + k_{6\perp} \sin^6\theta + k_{6||} \cos 6\phi \sin^6\theta + \dots$$

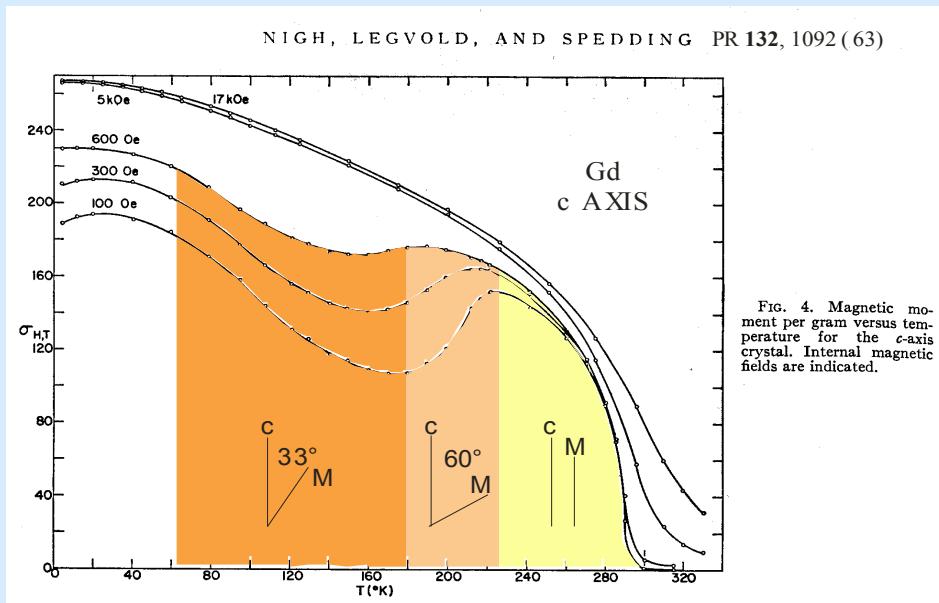
**each  $K_i$  has a „volume“ and „surface“ contribution**

$$K_i = K_i^V + 2K_i^S/d$$

M. Farle Rep. Prog. Phys. **61**, 755 (1998)

K. B. Handb. Magn. Magn. Mat. **3**, 1617 (2007) # see web

# Spin reorientation in bulk ferromagnets



Gd ist **not** isotropic, it has  $K_2, K_4, K_6 \neq 0$

SRT for hcp Co  
 $\sin\theta = (K_2/2K_4)^{1/2}$

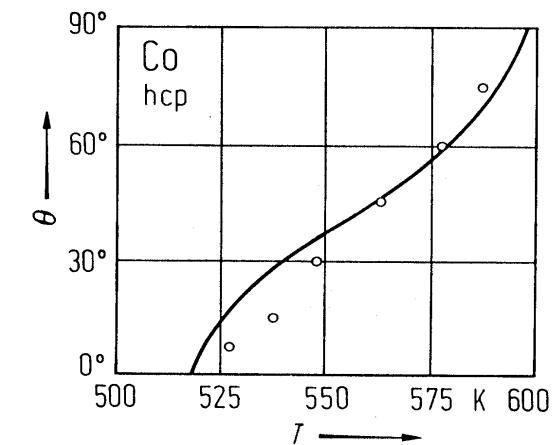


Fig. 5. Temperature dependence of the angle  $\theta$  between the direction of spontaneous magnetization and the *c* axis of a single crystal of hcp Co [61 B 5]. Points: data. Curve: calculated from  $\sin\theta = (-K_1/2K_2)^{1/2}$ .

LB III, 19a, p.45

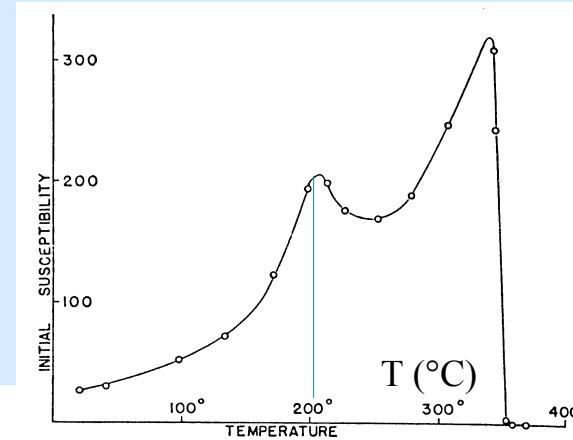
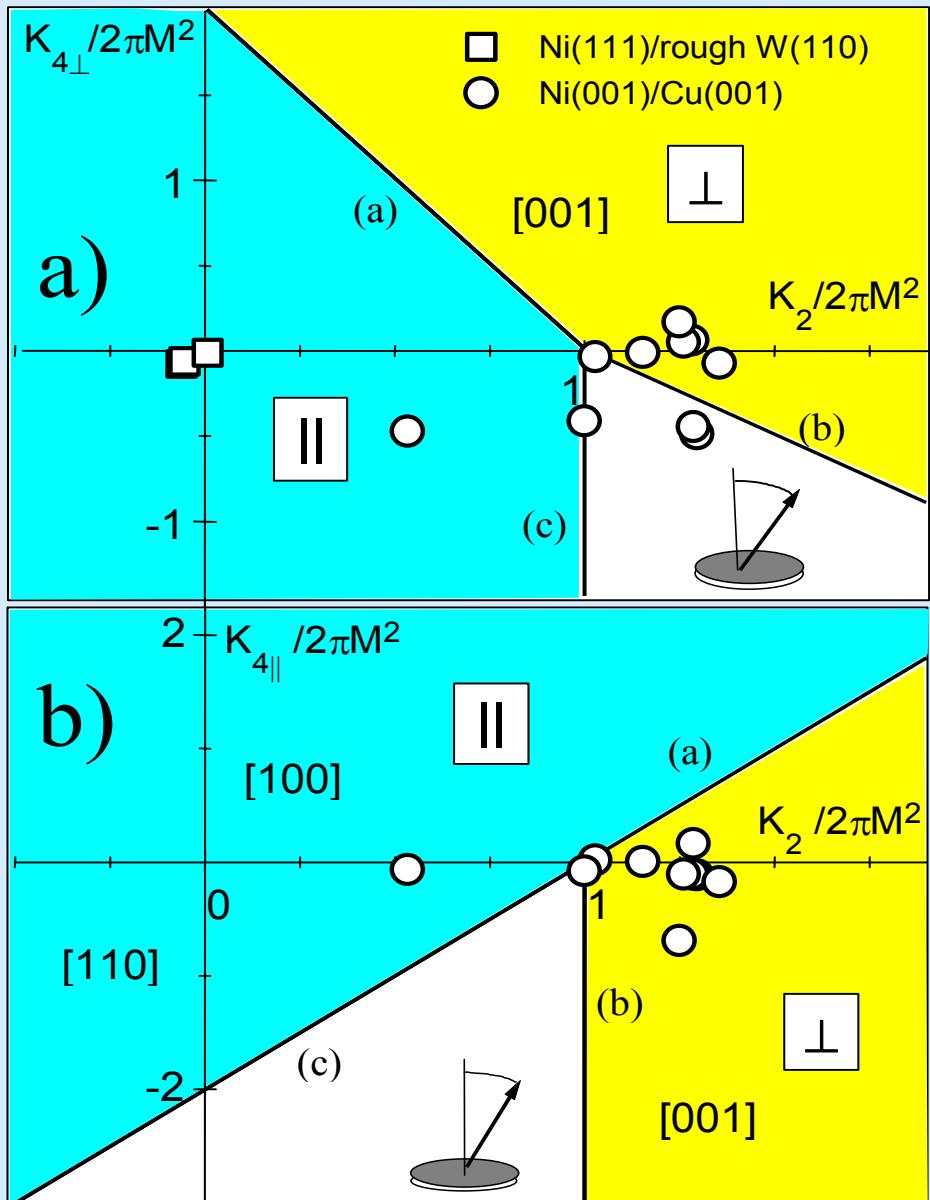


Fig. 6. The variation of the initial susceptibility with temperature in nickel.

# SRT in ultrathin Ni films



A. Berghaus, M. Farle, Yi Li, K. B.  
 Second Intern. Workshop on the Magnetic Properties  
 of Low-Dimensional Systems.  
 Proc. in Physics **50**, 61 (1989) #108

M. Farle et al., PRB **55**, 3708 (1997) #176  
 Only with  $K_4 \neq 0$  a continues SRT is possible!

$$\sin\theta = (K_2/2K_4)^{1/2}$$

Do not use  $K_{\text{eff}} = 2\pi M^2 - K_i \dots$   
 because  $f(T)$  and  $g(T)$  are different.  
 Use the ratio  $K_i / 2\pi M^2 \Rightarrow f(T) / g(T)$

What causes the SRT?

There is only **one** reason, the  $K_i(T, d)$ !

Higher order MAE  $K_i$

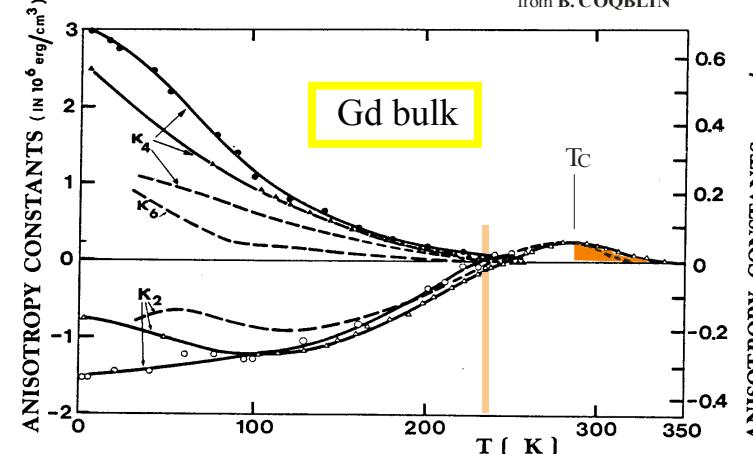
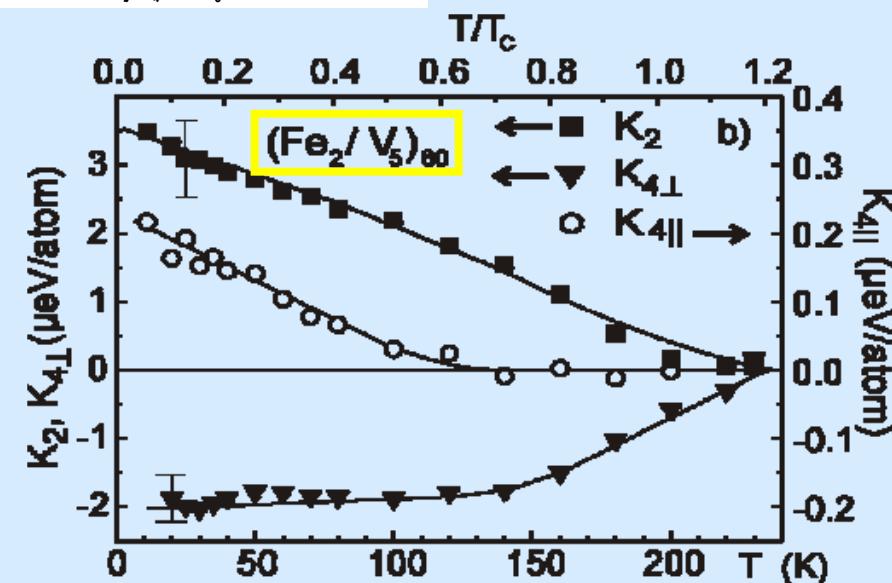
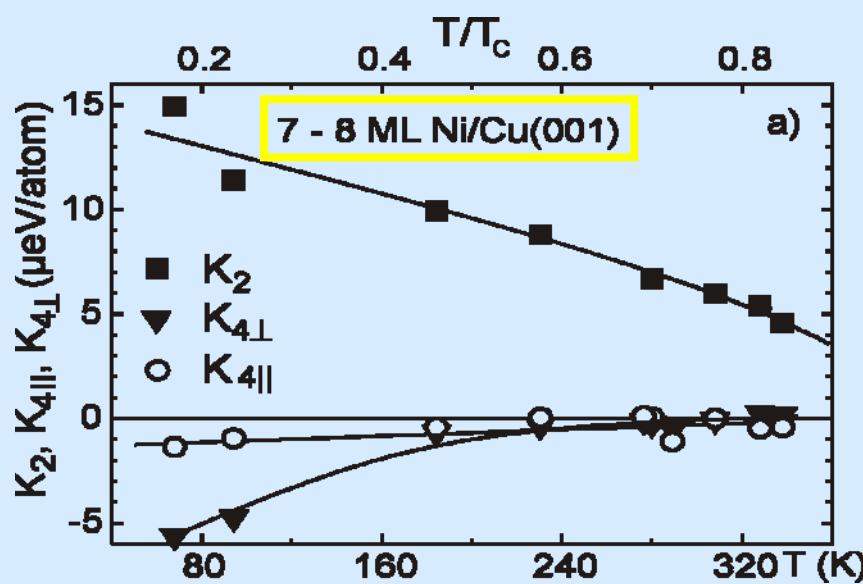


Fig. 160. Experimental values of the anisotropy constants  $\kappa_2$ ,  $\kappa_4$  and  $\kappa_6$  versus temperature in Gadolinium. The circles ( $\circ$  for  $\kappa_2$ ,  $\bullet$  for  $\kappa_4$ ) represent the data of Feron (Fig. 11 of Ref. 280), the triangles ( $\Delta$  for  $\kappa_2$ ,  $\blacktriangle$  for  $\kappa_4$ ) the data of Graham (Fig. 1 of Ref. 66) and the full lines connect respectively the data of Feron and those of Graham. The dotted lines give the data of Corner *et al.* (Fig. 5 of Ref. 70 modified by Ref. 661) for  $\kappa_2$ ,  $\kappa_4$  and  $\kappa_6$ .



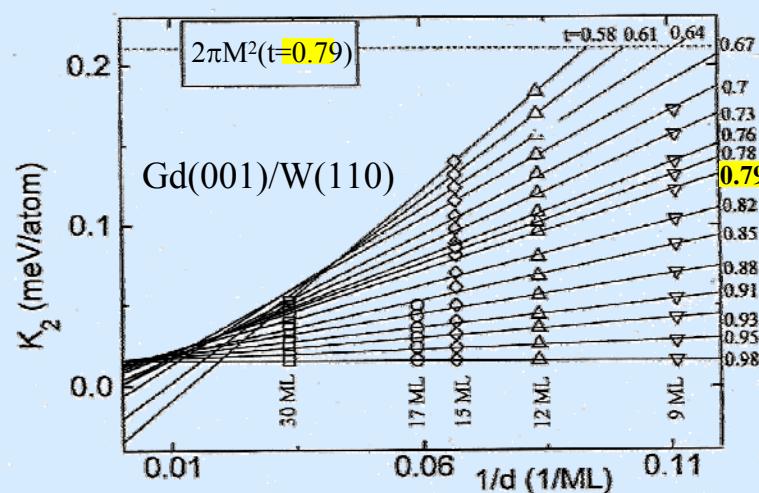
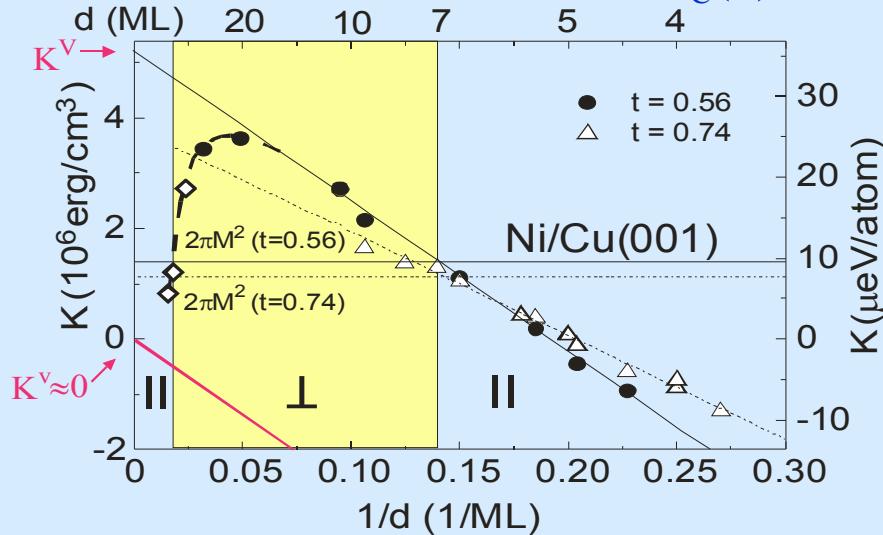
Ni is the only 3d ferromagnet for which  $T_C(d)$  is measured over the full range of temperature and thickness

To analyze SRT in thin films is difficult and tedious because there is a  $T$  and  $1/d$  dependence:

$$T / T_C(d)$$

and

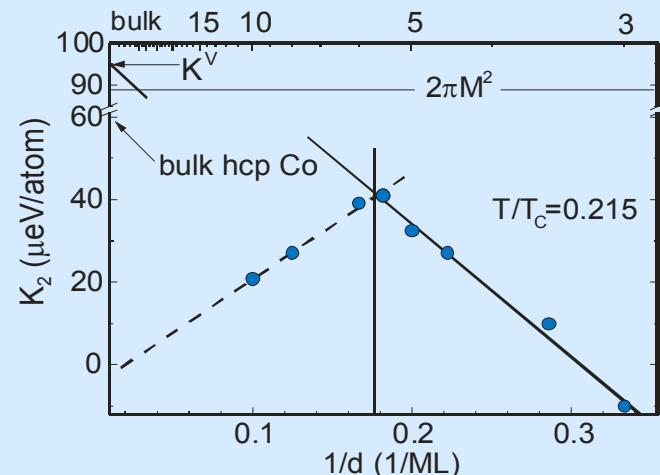
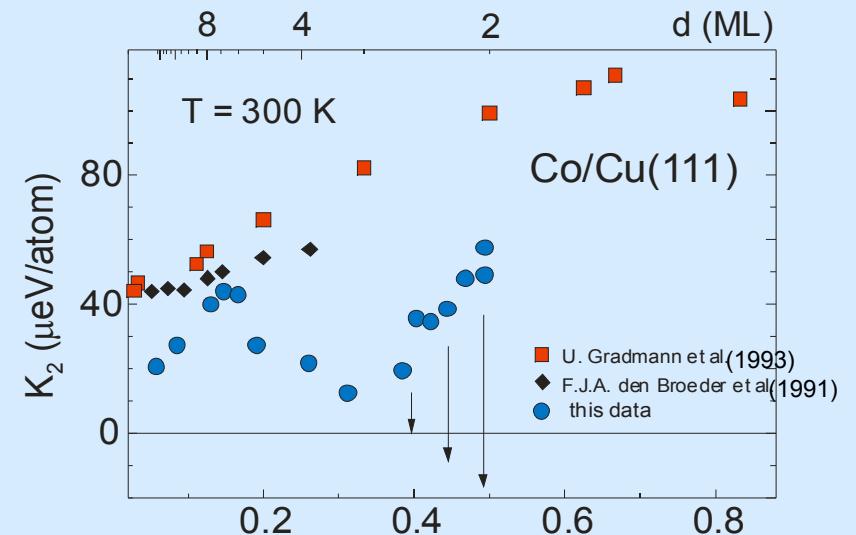
$$K(T) = K_V(T) + 2K_S(T)/d$$



G. André et al., Surface Science **326**, 275 (1995)  
 K. B. and M. Farle, J. Appl. Phys. **81**, 5038 (1997)

Why  
does Ni  
undergo  
a SRT  
and  
Co not ?

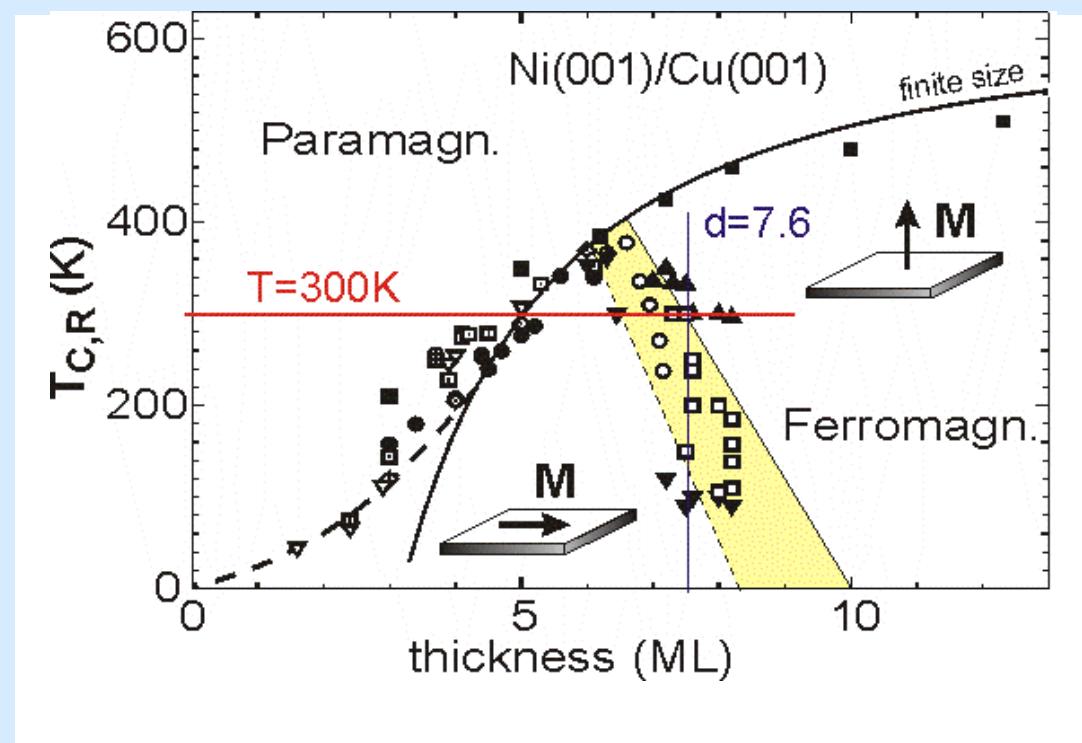
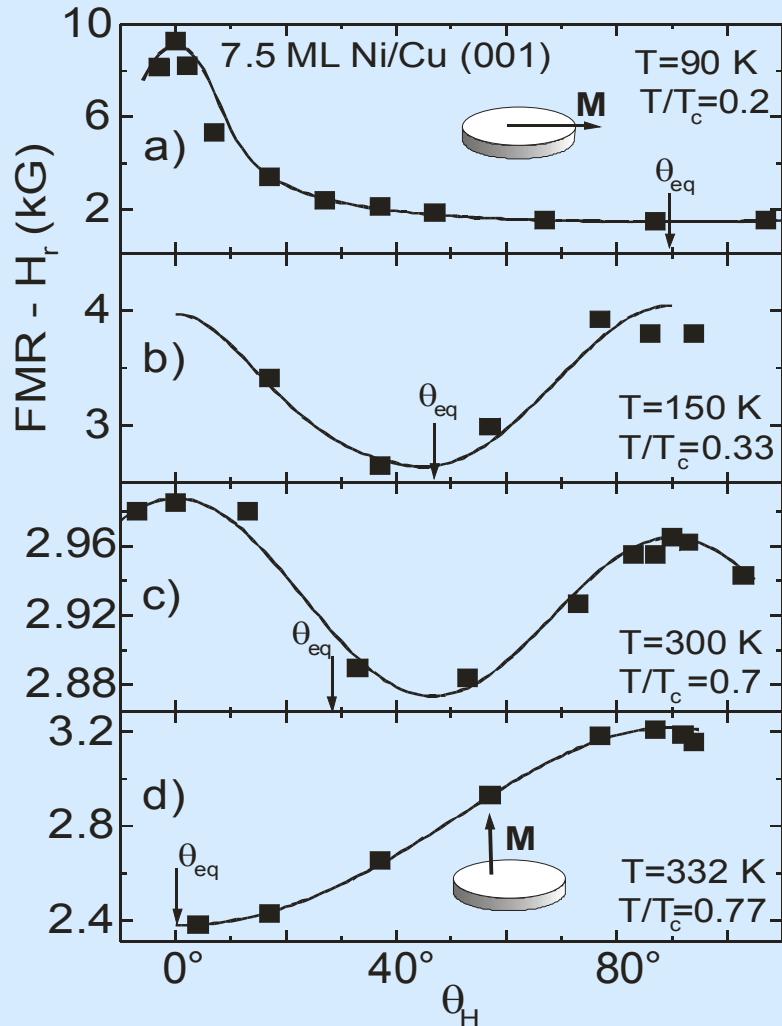
=> #330



M. Farle et al., Surf. Sci. **439**, 146 (1999)

In a proper analysis, taking  $T/T_C(d)$  in consideration, we always find a linear  $K = K_V + 2K_S/d$  dependence.  
 A departure from this “Néel argument” indicates changes in the x-tal structure.

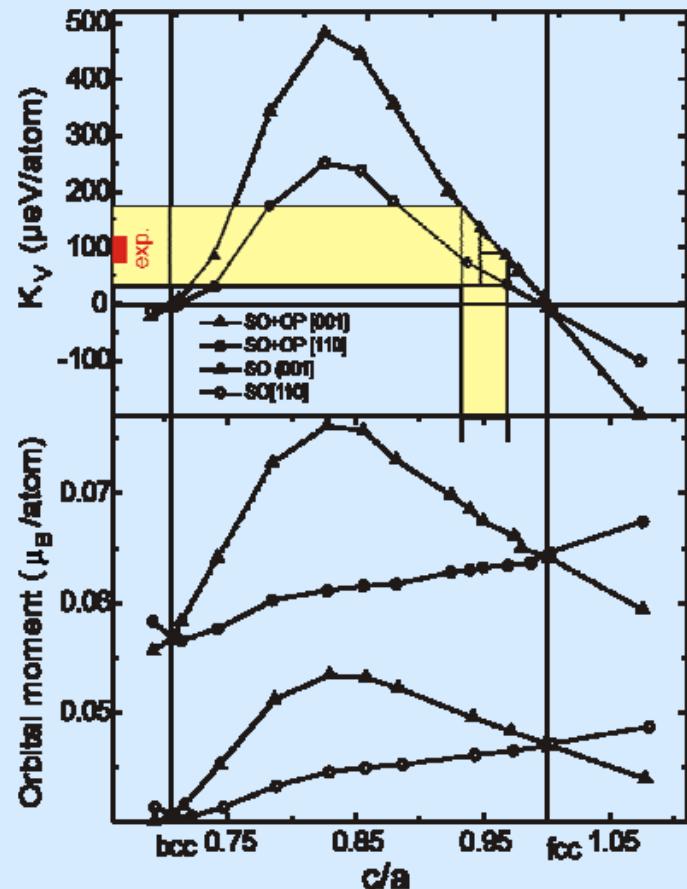
# Experimental FMR evidence for a continuous rotation



Farle et al. PRB **56**, 5100 (1997) #185

SRT is caused by the temperature dependence of  $K_i(T)$ .

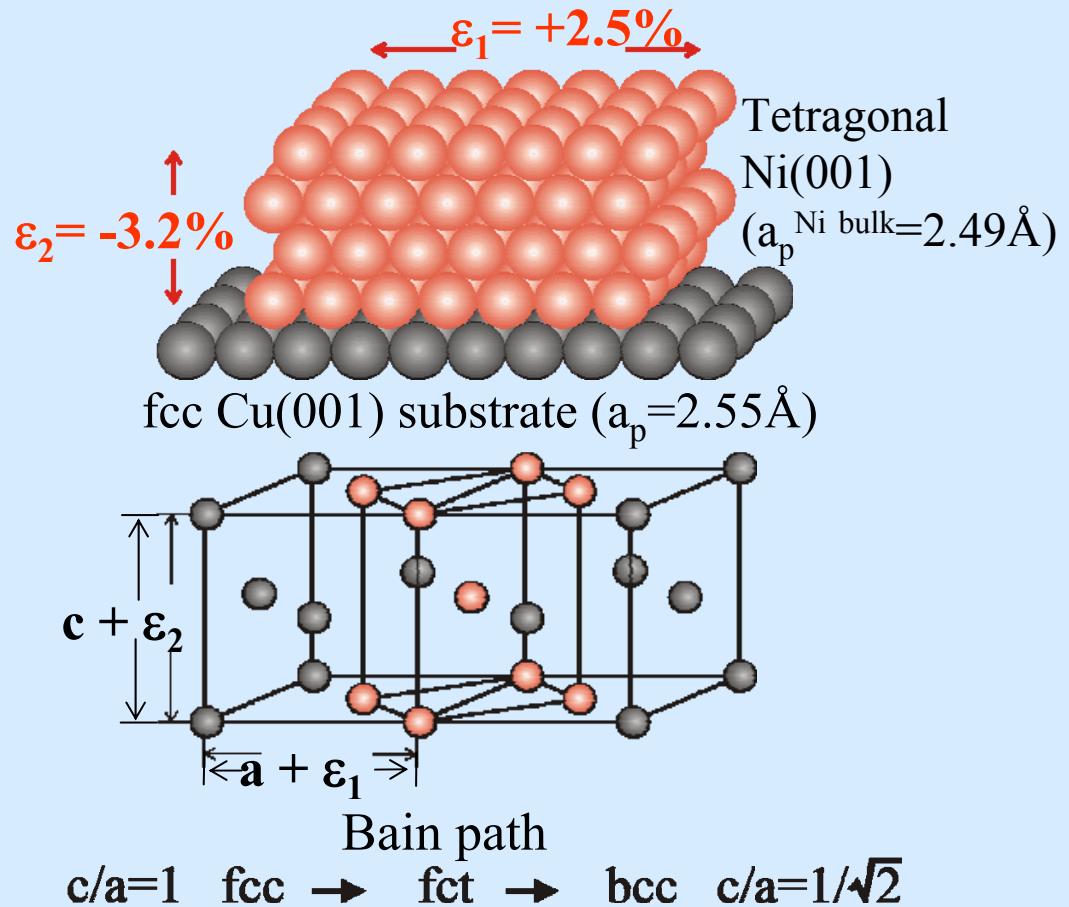
# Hypothetical structure in theory



Structural changes by  $\approx 0.05 \text{ \AA}$  increase MAE by 2-3 orders of magnitude ( $\sim 0.2 \rightarrow 100 \mu\text{eV/atom}$ )

O. Hjortstam, K. B. et al. PRB **55**, 15026 ('97)  
R. Wu et al. JMMM **170**, 103 ('97)

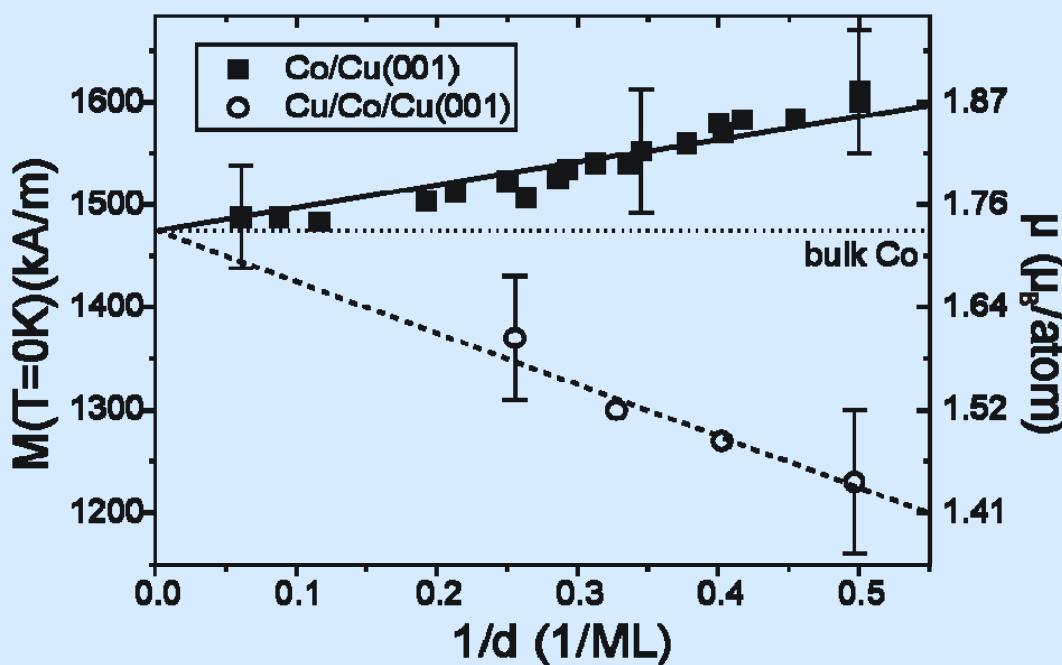
Growth of artificial nanostructures  
bcc, fcc  $\rightarrow$  tetragonal, trigonal



# Manipulation of SRT

## Magnetic moments at surface/interface

### UHV-SQUID measurements



Theory:

Hjortstam et al., PRB **53**, 9204 (1996)

Pentcheva et al., PRB **61**, 2211 (2000)

$$m_{\text{tot}} = m_{\text{vol}} + \frac{m_{\text{surf}} + m_{\text{inter}} - 2}{d} \quad (\text{linear with } 1/d)$$

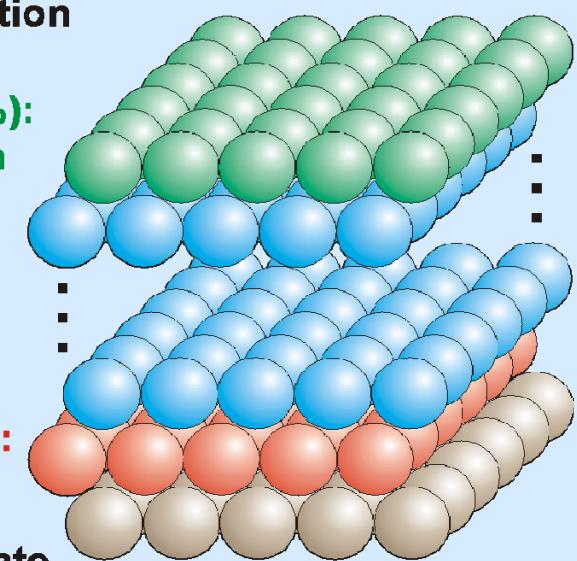
### Co moment distribution

Surface (+32(5)%):  
 $2.28(8) \mu_B/\text{atom}$

bulk  
 $\mu = 1.73 \mu_B$

Interface (-17(3)%):  
 $1.43(5) \mu_B/\text{atom}$

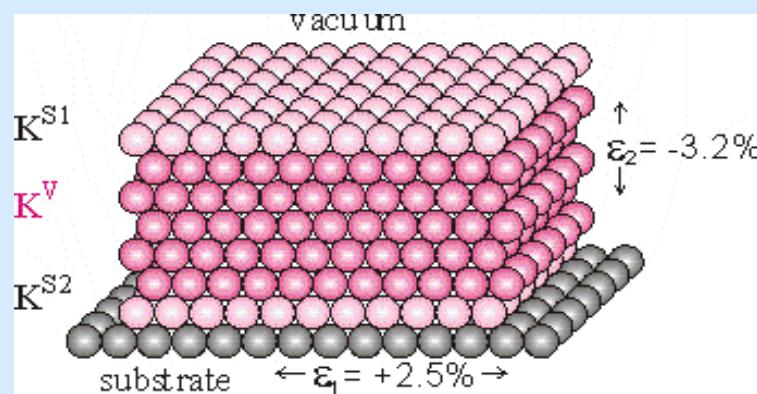
Cu substrate



A. Ney et al.

Europhys. Lett. **54**, 820 (2001)

# Ni/Cu(001)

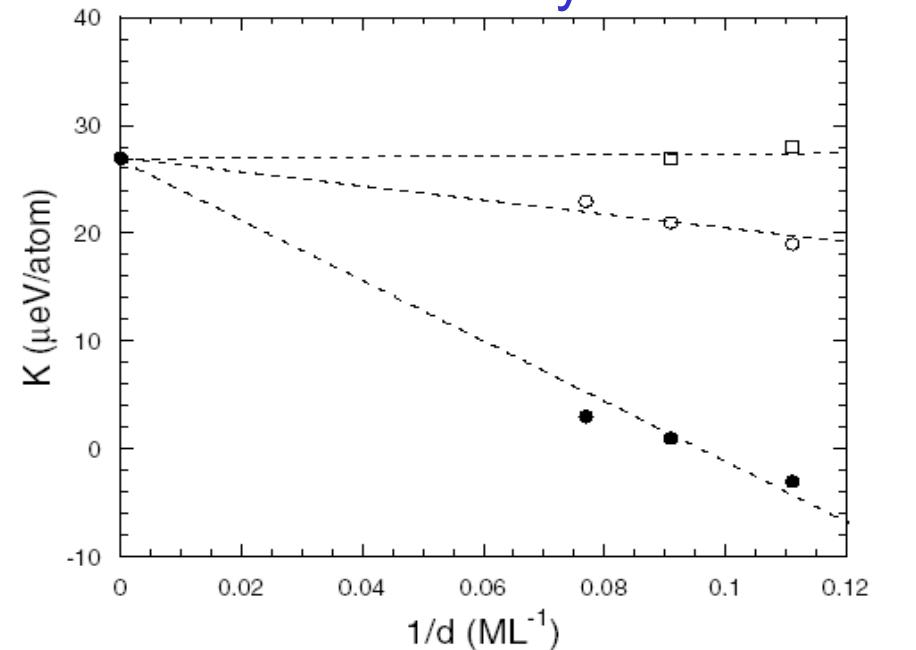
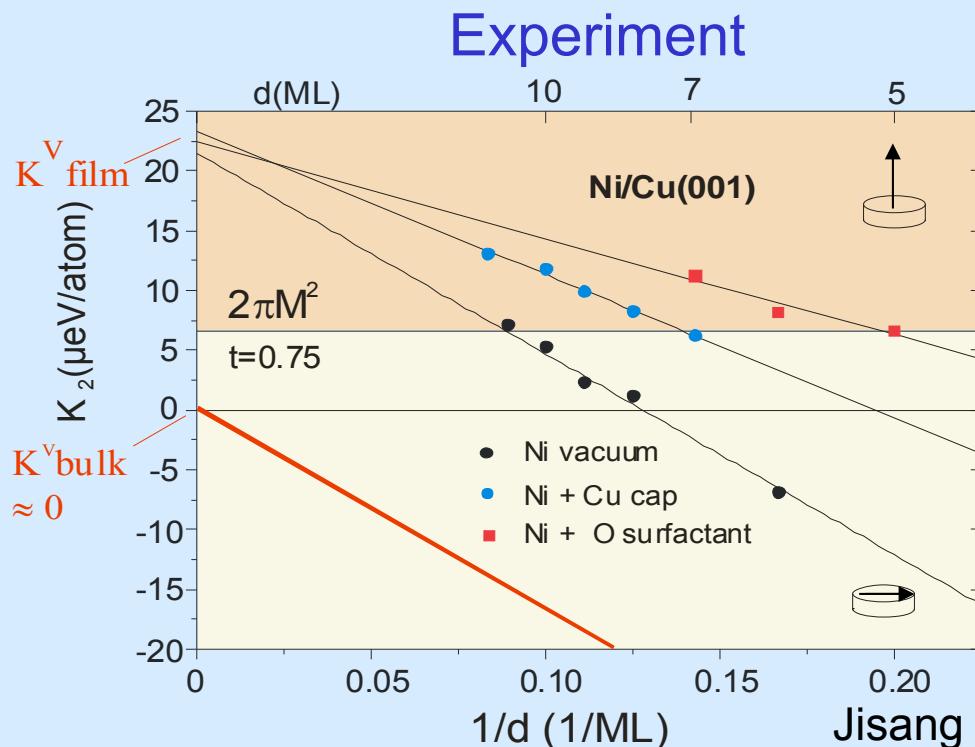


$$F \sim (2\pi M^2 - K_{2\perp}) \cos^2 \theta$$

$$K = K^V + \frac{K^{S1} + K^{S2}}{d}$$

Interface	$K_s$ ( $\mu\text{eV}/\text{atom}$ )	$d_c$ (ML)
Ni/vacuum	-107	10.8
Ni/Cu	-59	7.6
Ni/CO (van Dijken et al.)	-81	7.3
Ni/H <sub>2</sub> (van Dijken et al.)	-70	6.8
Ni/O (surfactant)	-17	4.9

## Theory



Jisang Hong et al., Phys. Rev. Lett. **92**, 147202-1 (2004)

## Effect of postgrowth oxygen exposure on the magnetic properties of Ni on the Cu-CuO stripe phase

M. Denk, R. Denk, M. Hohage, L. D. Sun, and P. Zeppenfeld\*

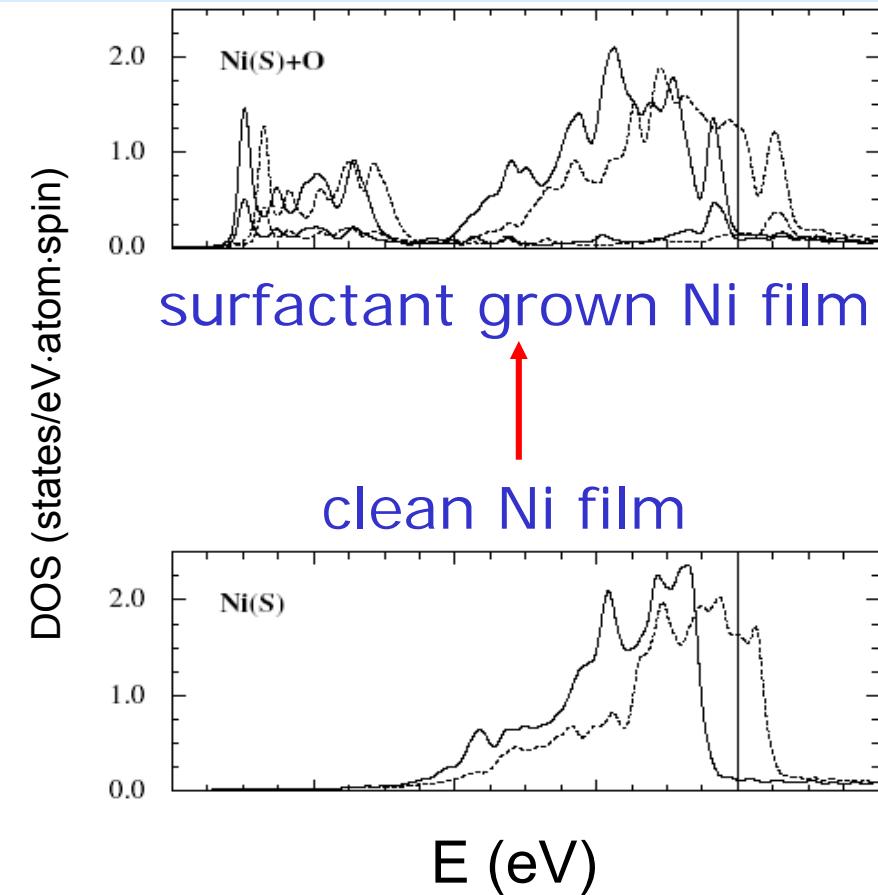
*Institute of Experimental physics, Johannes Kepler University Linz, Altenbergerstr. 69, 4040 Linz, Austria*

(Received 3 August 2011; revised manuscript received 18 November 2011; published 23 January 2012)

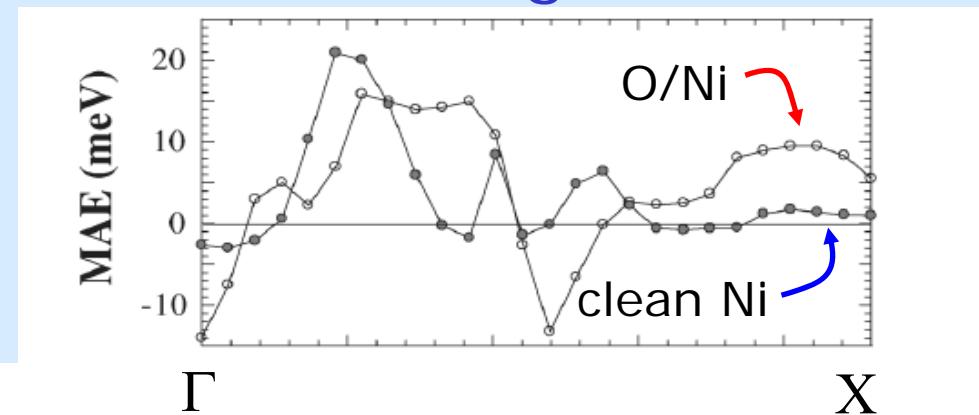
The magnetism and morphology of thin Ni films deposited on the Cu(110)-Cu(110)-(2 × 1)O surface (Cu-CuO stripe phase) have been studied by scanning tunneling microscopy (STM) and reflectance difference magneto-optical Kerr spectroscopy (RD-MOKE). The magnetic easy axis of the Ni films lies completely in plane up to a coverage of 22.5 ML. Exceeding this coverage, a small remanent magnetization component pointing out of plane evolves. Upon postgrowth oxygen exposure the Ni film becomes completely out-of-plane magnetized and the out-of-plane remanence and coercive field strongly increase during exposure. STM images reveal a fully (2 × 1)O reconstructed topmost Ni layer after the oxygen exposure, but no morphological changes of the Ni film. We thus conclude that the oxygen-induced surface reconstruction strongly modifies the magnetic properties of the Ni film by enhancing the surface magnetic anisotropy.

# Results of ab initio calculations for O/Ni/Cu(001)

## Density of states



## MAE along $\overline{\Gamma X}$ axis

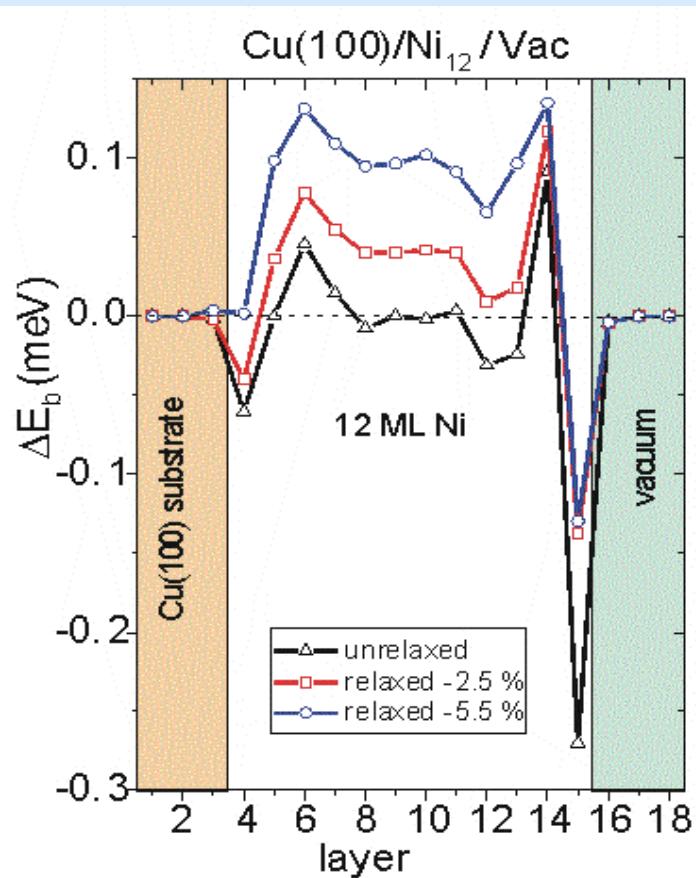


- DOS shows that topmost Ni moment is basically unchanged
- O-induced surface state seen in the vicinity of X-point is responsible for change in MAE
- theory reveals induced moment in surfactant oxygen

Jisang Hong et al., *Phys. Rev. Lett.* **92**, 147202-1 (2004)

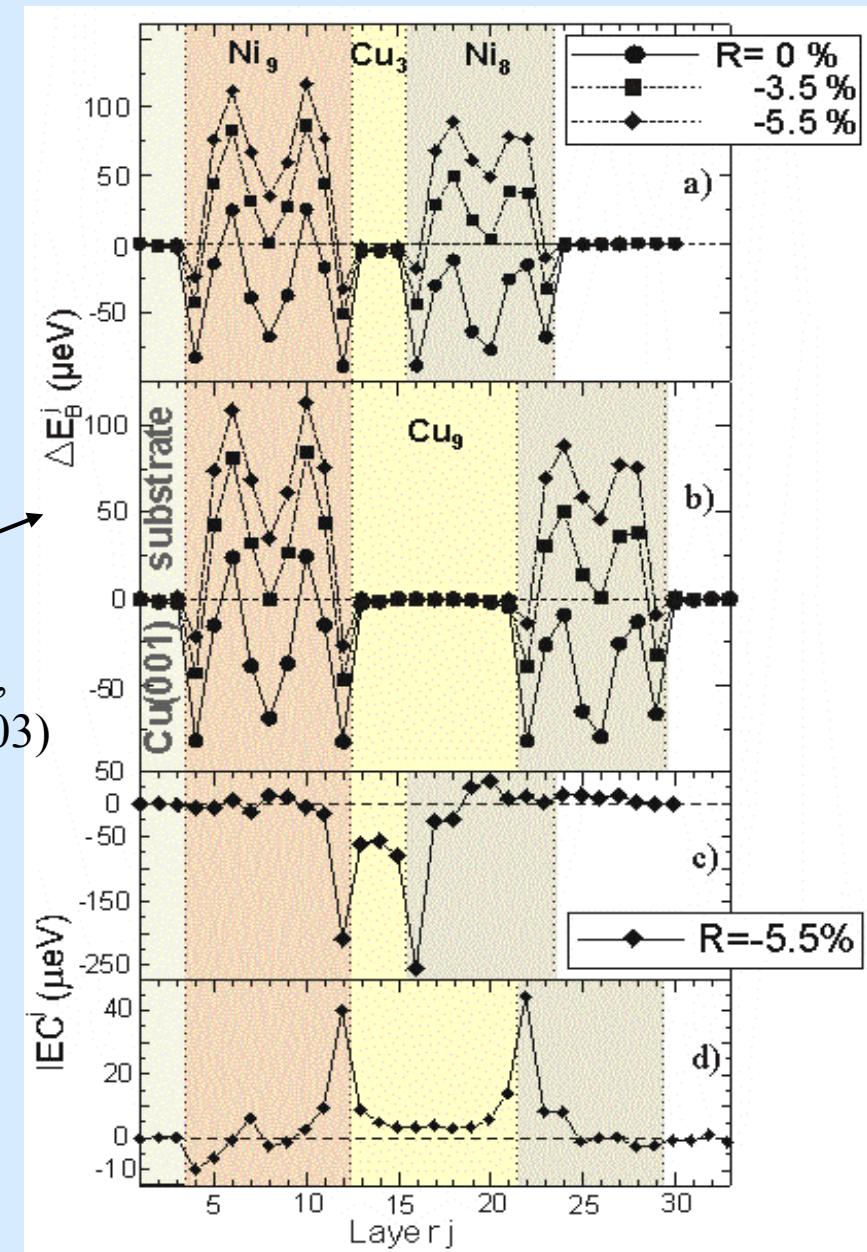
# SP-KKR calculation for right fcc and relaxed fct structures

layer resolved  $\Delta E_b = \sum K_i$  at T=0



C. Uiberacker et al.,  
PRL **82**, 1289 (1999)

R. Hammerling et al.,  
PRB **68**, 092406 (2003)



The surface and interface MAE are certainly large (L. Néel, 1954) but count only for one layer each. The inner part (volume) of a nano-structure will overcome this, because they count for n-2 layers.

# Summary

A whole variety of experiments on nanoscale magnets are available nowadays. Unfortunately many of the data are analyzed using theoretical *static mean field (MF) model*, also textbook for *Untrathin Magnetic Structures* use the bulk magnetism approach.

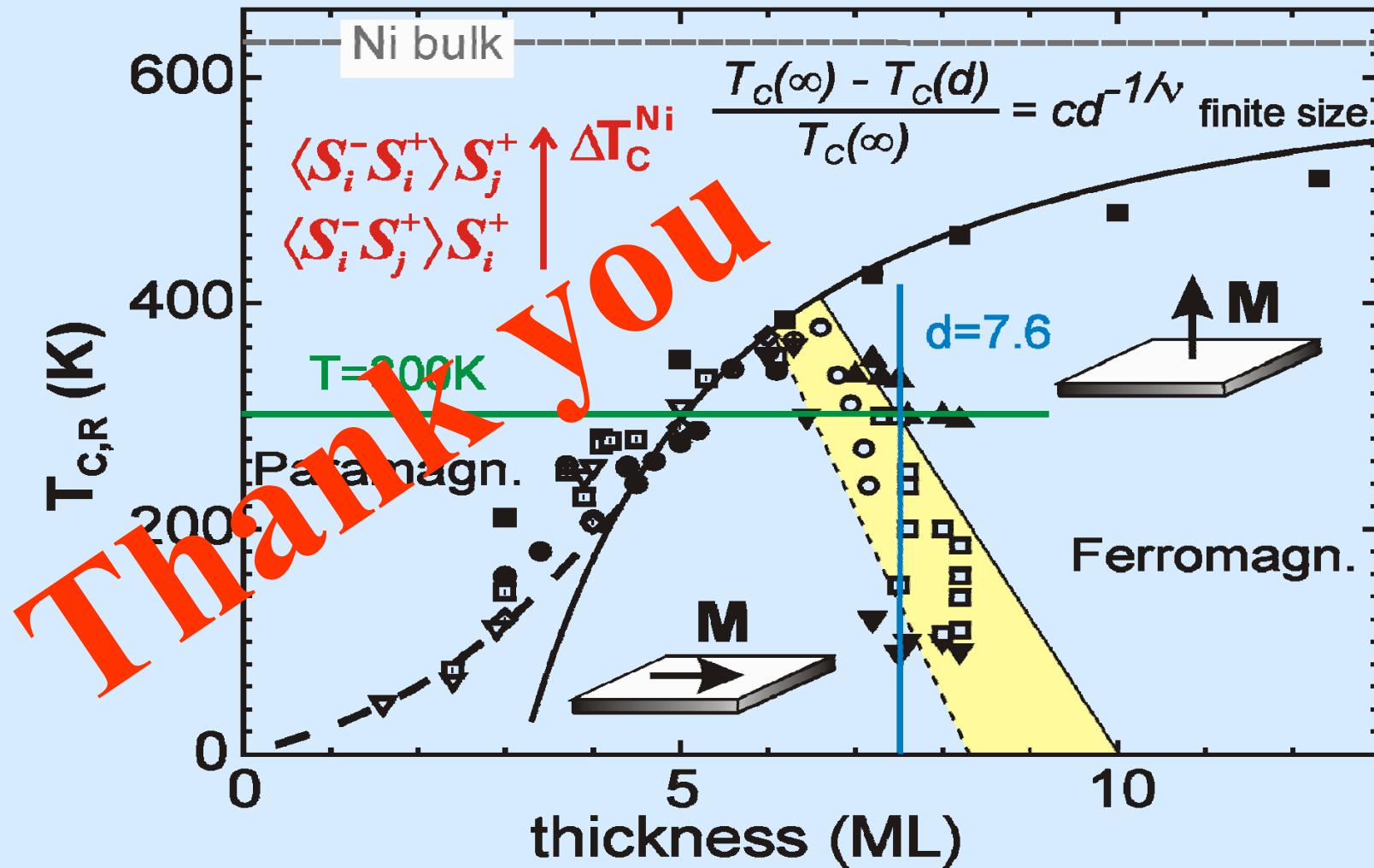
Such a mean field ansatz is insufficient for nanoscale magnetism, we demonstrate the importance of *higher order spin-spin correlations* in low dimensional magnets.

The spin is not a good quantum number, it ignores the orbital magnetism.  
The orbital magnetic moment creates the MAE.  
And the MAE manipulates the SRT.

## Conclusion:

**The magnetism of FM monolayers is a very reach playground  
and a fruitful collaboration between theory and experiment.**

# Take Home Cartoon



<http://www.physik.fu-berlin.de/~bab>

(#xyz see publ.list)

# Phase transitions in ferromagnetic monolayers: A playground to study fundamentals

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Ultrathin ferromagnetic films of few atomic layers of Fe, Co, Ni, or Gd, etc. allow manipulations of the magnetism which is hardly accessible in the bulk: (i) Due to special growth mechanisms, crystallographic structures can be prepared which is impossible in bulk magnetism, e. g. tetragonal Ni. (ii) As a consequence of the *finite size effect* one can shift the phase transition temperature  $T_C$  to almost any value between zero and the bulk Curie-temperature as function of the film thickness  $T_C(d)$ . (i) Changes of the c/a ratio by a few percent, or  $\approx 0.05\text{\AA}$  of the nearest neighbour distance will change the magnetic anisotropy energy (MAE) by orders of magnitude. With these changes we are in a position to manipulate the spin reorientation transition (SRT). We will discuss its physical origin and distinguish between a continuous rotation of the easy axis of the magnetization versus a sudden switch from in-plane to out-of-plane. (ii) The variable phase transition temperature  $T_C(d)$  allows to shift  $T_C$  to a convenient temperature range and to study critical phenomena close to  $T_C$ , e. g. the critical exponents  $\beta$  and  $\gamma$  as well as the dimensional crossover from 3D $\rightarrow$ 2D. We will discuss several experimental techniques its strength and pitfall (MOKE, spin-polarized PE, magnetic resonance [1,2], ac-susceptibility [3], etc.) and some of the recent results.

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